



BCA (Part-I) Examination, 2022

# Paper - I

*Time : Three Hours]                      [Maximum Marks : 80*

**Note** : Answer any **two** parts from each question. All questions carry equal marks.

## Unit-I

1. (a) (I) If  $p \equiv$  Ramesh is a player  $q \equiv$  Mohan is wise, then write the following symbols in sentence :
  - (i)  $\sim p \vee \sim q$
  - (ii)  $\sim (p \wedge q)$

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(II) Write the following sentences in symbols :

- (i) Until Sheela will not come I shall not go to college.
- (ii) When Sheela will come then I shall go to college.

(III) Write True or False of the following statements :

- (i)  $\{2, 3\} \subset \{2, 4, 6\}$
- (ii)  $5 \in \{1, 3, 5\}$

(IV) Are the following propositions ?

- (i) Some roses are black.
- (ii) May you live long.

(b) Prove that  $(p \Leftrightarrow q) \wedge (q \Leftrightarrow r) \Rightarrow (p \Leftrightarrow r)$  is a Tautology.

(c) (I) If  $Q(x) = x$  is a rational number.

$R(x) = x$  is a real number.

then translate the following sentences into symbols :

- (i)  $R$  is a real number.
- (ii) Every rational number is a real number.

(II) Negate each of the following statements :

- (i)  $\forall x (|x| = x)$
- (ii)  $\exists x (x + 2 = x)$

- (III) Write the following predicate into symbols and also write its negative in symbols. "Every rational number is a real number."

### Unit-II

2. (a) (I) In a Boolean algebra  $B$ , the identity elements are complementary to each other i. e., for  $0, 1 \in B$ , then show that :

(i)  $0' = 1$

(ii)  $1' = 0$

- (II) In a Boolean algebra, show that if  $a + b = a + c$  and  $ab = ac$ , then  $b = c$ .

- (b) (I) Show that the order relation  $\leq$  is partial order relation in a Boolean algebra.

- (II) In a Boolean algebra  $B$ , if  $x \leq y$  and  $y \leq x$ , then prove that  $x = y$ .

- (c) (I) Construct a circuit for the Boolean function

$$F(a, b, c) = a \cdot b \cdot c + a' \cdot b \cdot c$$

Simplify it and draw the figure.

- (II) Draw the logic circuit with inputs  $a, b, c$  and output  $X$  where

$$X = abc + a'c' + b'c'$$

**Unit-III**

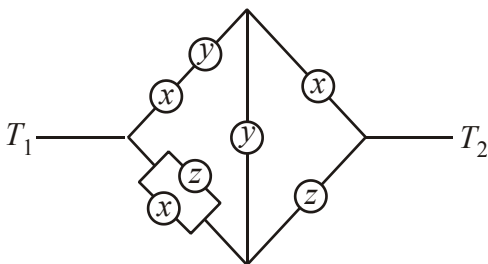
3. (a) (I) Express the following function in disjunctive normal form in the smallest possible number of variables :

$$f(x, y, z) = xy' + xz + xy$$

- (II) Express the following function in conjunctive normal form :

$$f(x, y, z) = (xy' + xz)' + x'$$

- (b) (I) Simplify the following circuit.



- (II) Design a 3-terminal circuit which gives the real forms to the following functions :

$$f = xzw + y'zw$$

$$g = xzw + y'zw + x'y'z$$

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- (c) (I) Draw the binomial net for the following flow functions :

$$x \cdot y \cdot z + x' \cdot y \cdot z + xy'z + x'y'z'$$

- (II) Design a tree-net in three variables for the flow function :

$$xyz + x'yz + xy'z + x'y'z$$

**Unit-IV**

4. (a) (I) If  $A = \{1, 2, 3\}$ ,  $B = \{2, 4\}$  and  $C = \{3, 5\}$ , then find  $A \times (B - C)$ .

- (II) If  $A = \{1, 2\}$ ,  $B = \{2, 3\}$  and  $C = \{3, 5\}$ , then find

$$(A \times B) \cap (A \times C).$$

- (b) (I) Let  $A = \{1, 2, 3, 4\}$  and  $B = \{a, b, c\}$  and let

$$R = \{(1, a), (2, a), (2, b), (3, a), (3, b)\}$$

be a relation from  $A$  to  $B$ , then find  $R^{-1}$ ,  $d(R)$ ,  $r(R)$ ,  $d(R^{-1})$  and  $r(R^{-1})$

- (II) Is the relation 'is less than' transitive in the set of natural numbers ?

- (c) (I) Prove that the following sets are countable :

(i) the set  $I$  of all integers ;

(ii) the set  $E$  of all positive integers.

- (II) If  $A = \{1, 3, 5\}$ ,  $B = \{a, b, c\}$  and  $1 \leftrightarrow a$ ,  $3 \leftrightarrow b$ ,  $5 \leftrightarrow c$ , show that it is one-one onto mapping.

**Unit-V**

5. (a) (I) Show that the vertices of odd degree (odd vertices) in a graph is always even.

(II) Draw the equivalent labelled graphs for  $G_1$  and  $G_2$  if

$$G_1 = \{\{v_1, v_2, v_3\} \{v_1, v_2\} \{v_1, v_3\} \{v_2, v_3\}\}$$

$$G_2 = \{\{w_1, w_2, w_3\} \{w_1, w_2\} \{w_1, w_3\} \{w_2, w_3\}\}$$

(b) (I) Draw the graphs represented by the following adjacency matrices :

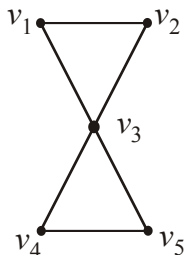
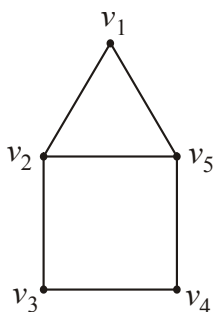
$$\begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}$$

(II) Express the following algebraic expressions in binary trees :

$$(x - y) + ((y + z) + w)$$

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(c) (I) Which of the following graphs have a Hamiltonian circuit ?



(II) A graph with at least one edge is 2-chromatic if and only if it has no circuits of odd length.